

1 **TITLE:** CProb: A Computational Tool for Conducting Conditional Probability Analysis

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14 **ABBREVIATION LIST:** Conditional Probability Analysis (CPA), National Land Cover Dataset  
15 (NLCD), Environmental Monitoring and Assessment Program (EMAP)

16

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1 **Abstract:**

2 Conditional probability measures the probability of observing one event given that another event  
3 has occurred. In an environmental context, conditional probability helps to assess the association  
4 between an environmental contaminant (i.e., the stressor) and the ecological condition of a  
5 resource (i.e., the response). These analyses, when combined with controlled experiments and  
6 other methodologies, show great promise in evaluating ecological conditions from observational  
7 data and in defining water quality and other environmental criteria. Current applications of  
8 conditional probability analysis are largely done via scripts or cumbersome spreadsheet routines,  
9 which may prove daunting to end users and do not provide access to the underlying scripts.  
10 Combining spreadsheets with scripts eases computation through a familiar interface (i.e.,  
11 Microsoft Excel) and creates a transparent process through full accessibility to the scripts. With  
12 this in mind, we developed a software application, CProb, as an Add-in for Microsoft Excel with  
13 R, R(D)com Server, and Visual Basic for Applications. CProb calculates and plots scatterplots,  
14 empirical cumulative distribution functions and conditional probability. In this short  
15 communication, we describe conditional probability analysis, our motivation in developing a  
16 conditional probability analysis tool, its implementation as a Microsoft Excel Add-in, and  
17 illustrate its use with an example focusing on water quality criterion. CProb is freely available  
18 for download from <http://www.epa.gov/emap/nca/html/regions/cprob>.

19

20 **Keywords:** Conditional probability analysis; Water quality criteria; Stressor-response  
21 associations; Causal analysis; The R Project for Statistical Computing; R(D)COM server; RExcel

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## 1 INTRODUCTION

2           A goal of many applied environmental science efforts is to understand the association  
3 between environmental pollutants (i.e., stressors) and ecological condition (i.e., response).  
4 Understanding this relationship helps to identify areas of likely ecological impairment, explore  
5 potential causes and consequences of those impairments, and set acceptable levels of a given  
6 stressor so that the health of an ecosystem may be protected. It is possible to use both field and  
7 laboratory methods to explore stressor-response relationships and set criteria that are protective of  
8 ecological condition. Inference based on field survey data alone can be problematic because of  
9 confounding, uncontrolled variation in field experiments. Conversely, controlled laboratory  
10 experiments alone are unable to replicate the full range of factors that affect ecosystems. Causal  
11 assessment is an approach that combines field survey information from independent datasets and  
12 lab and field experimental results to develop multiple lines of evidence that elucidate these  
13 associations (Angradi, 1999; US EPA, 2000). An example of the causal assessment strategy is  
14 found in a recent document on developing water quality criteria for suspended and bedded  
15 sediments (US EPA, 2006). A key component of this approach is Conditional Probability  
16 Analysis (CPA) which was identified as having significant promise and has been used elsewhere  
17 to develop possible water quality criteria and explore ecological condition – human health  
18 associations (Paul and McDonald, 2005, Paul et al. In Press).

19           In our experience, causal assessment and CPA are well received by many state  
20 environmental managers; however, a common stumbling block for implementation is access to  
21 user-friendly software. As such, we developed a computational tool that uses Microsoft Excel®  
22 as an interface and the R Language for calculating and plotting conditional probabilities. In this  
23 short communication we describe CPA, our motivation for developing a CPA software tool, and  
24 demonstrate the use of the tool with two examples: a water quality criterion example from Paul

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1 and McDonald (2005) and, building on prior work, a landscape ecological example (Comeleo et  
2 al., 1996; Paul et al., 2002; Hollister et al., 2008a; 2008b)

3

#### 4 *Conditional Probability Analysis*

5 A conditional probability is the probability of an event Y occurring given that some other  
6 event X also has occurred. It is denoted P (Y|X). Thus, a conditional probability describes the  
7 probability of observing an event of interest in a subset of samples drawn from the original  
8 statistical population. These subsets are defined by conditions when X has occurred, in addition  
9 to those used to define the entire statistical population. Conditional probability is calculated as  
10 the ratio of the joint probability that Y and X occur simultaneously in a given sample from the  
11 original statistical population (P(Y, X )), to the probability of X in the original population. The  
12 notation for this is written:

$$13 \quad P(Y | X) = \frac{P(Y, X)}{P(X)} \quad (1)$$

14 The possible applications of conditional probability are very broad. We focus on the more  
15 limited context of environmental condition, in which conditional probability may be interpreted  
16 as the probability of environmental or ecological impairment given a pollutant, nutrient, or other  
17 stressor is larger or smaller than a certain amount (e.g., the probability of benthic community  
18 impact given copper concentration in sediments exceed 10 ppm). Refer to Paul and McDonald  
19 (2005) for additional information.

20

#### 21 *Motivation for developing a Conditional Probability Analysis Tool*

22 CPA usually involves informal spreadsheet routines or scripts. The spreadsheet routines  
23 require a high degree of user interaction, which increases the potential for transcription errors,  
24 incorrect formulas and may lead to an overall decline in the reproducibility of the analysis.

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1 Scripts improve reproducibility and reliability, but are much less accessible as they require  
2 statistical programming languages such as S-Plus® or R. While these software applications are  
3 quite robust and reliable, they suffer from either being quite expensive, in the case of S-Plus, or  
4 require a steep learning curve.

5 The anticipated end users of CPA are local or state environmental managers who have the  
6 technical expertise to understand CPA, but are unlikely to have the time to learn a new  
7 application. Additionally, these users often prefer spreadsheets such as Microsoft Excel® for  
8 statistical analysis and data management. Although the limitations of using spreadsheets for  
9 statistical analysis and for managing data are well documented ( Su et al., 2003; Knüsel, 2005;  
10 McCullough and Wilson, 2005), spreadsheets do provide a familiar interface for managers and  
11 provide a useful front end for other computational resources and new software tools ( Su et al.,  
12 2003; Baier and Neuwirth, 2007). With this in mind, we use the statistical programming  
13 language R to build a script to calculate CPA. We combine the script with the familiar front end  
14 of Microsoft Excel 2003®. We accomplish this with a CPA Excel Add-in, CProb, that uses the  
15 R(D)COM server and RExcel (Baier and Neuwirth, 2006a; 2006b; 2007; R Development Core  
16 Team, 2006).

17

## 18 **MATERIALS AND METHODS**

### 19 *Software requirements and installation information*

20 Freely available for download from <http://www.epa.gov/emap/nca/html/regions/cprob>,  
21 CProb version 1.0 is a Microsoft Excel® Add-in developed with Microsoft Office Excel 2003®,  
22 Visual Basic for Applications, R version 2.4.0, R(D)Com Server version 2.01 and RExcel version  
23 1.50. The Add-in uses Microsoft Excel® as a front end interface and calculates CPA using R as  
24 the statistical processor with R(D)Com providing the connection. Details about acquiring, using  
25 and installing these programs are available from Microsoft, The R Project for Statistical

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1 Computing, and the R(D)Com page at the University of Vienna, respectively (Table 1). Detailed  
2 installation instructions for CProb are in a README file (CProbREADME.txt) included with the  
3 download. Since development, new versions of R, R(D)Com Server and RExcel are available.  
4 and CProb is compatible with these.

5

### 6 *CProb Data Requirements*

7 Data with paired stressor and response variables are required to calculate CPA. The  
8 stressor is either a discrete or continuous variable such as dissolved oxygen concentration, density  
9 of suspended sediments, or number of landscape patches. The response is a dichotomous variable  
10 or a continuous or discrete variable transformed to a dichotomous variable (e.g., with a threshold)  
11 that is thought to be responsive to the stressor. For instance, Paul and McDonald (2005)  
12 compared percent fines in bedded sediments to probability of taxa richness of sensitive species  
13 less than a threshold. CProb also accepts inclusion probabilities (i.e., from data acquired with a  
14 probability sampling design) as an optional parameter. These probabilities are used to calculate  
15 unbiased estimators from the data for extrapolation to the statistical population from which the  
16 sample was drawn.

17 CProb does not accept non-numeric values and will return an error message. Non-  
18 numeric values must be corrected, removed, or converted to a missing value prior to running  
19 CProb. Allowable missing values are permissible with the missing value settings in RExcel (i.e.,  
20 either blank cells or “#N/A”). CProb will pass these to R and since paired data are required, the  
21 records with missing values are omitted from all calculations.

22

### 23 *Bootstrapped Confidence Intervals*

24 CProb uses standard bootstrap resampling to estimate the confidence intervals for the  
25 conditional probabilities (Manly, 2007). The raw data is resampled with replacement and a

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1 conditional probability is calculated for each bootstrap sample. The upper and lower confidence  
2 intervals are extracted as percentiles from the distribution of all bootstrapped conditional  
3 probabilities. The interval is determined by the “Confidence Interval Alpha” and the default  
4 value is 0.05. The default value for the number of bootstrap iterations is 100. This particular  
5 default value is provided to allow for an exploratory analysis that balances the interpretability of  
6 the analysis while limiting the demand for computational resources. One hundred iterations often  
7 results in unstable confidence intervals thus, the default value should only be used on initial,  
8 exploratory calculations. As a general rule of thumb, users of CProb should consider at least  
9 1000 iterations with an  $\alpha$  of 0.05 and 5000 iterations with an  $\alpha$  of 0.01 (Manly, 2007).

10

#### 11 *Water Quality Criterion Example*

12 To verify the output and test the functionality of CProb, we repeat the analysis conducted  
13 by Paul and McDonald (2005) for stream impairment and bedded sediments. In this example  
14 stream condition is defined by the total taxa richness of benthic macroinvertebrates in the orders  
15 Ephemeroptera (mayflies), Plecoptera (stoneflies), and Trichoptera (caddisflies) (i.e., EPT Taxa  
16 Richness). Bedded sediments are characterized by percentage fines in the substrate. Data for  
17 this example are from the U.S. EPA’s Environmental Monitoring and Assessment Program’s  
18 Mid-Atlantic Highlands Streams Assessment. See Paul and McDonald (2005) for details and  
19 additional references. The dataset for our example (included with the software download as  
20 “JEQData\_wq.csv”) includes records for 99 stations and contains four columns: Station Identifier  
21 (SITE.ID), Inclusion Probabilities (WGT.FS), EPT Taxa Richness (EPT.RICH), and Percentage  
22 of Embedded Fines (PCT.FN). We choose arguments to match the methodology in Paul and  
23 McDonald (2005) as closely as possible.

24

#### 25 *Landscape Example*

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1           To independently test CProb, we conduct a CPA between landscape metrics and the  
2 condition of estuarine sediments. It is accepted that developed lands impact the ecological  
3 condition of sediments in Mid-Atlantic estuaries of the United States (Comeleo et al., 1996; Paul  
4 et al., 2002; Hollister et al., 2008a; 2008b) . We use estuarine data (included with software  
5 download as JEQData\_le.csv) from the U.S. EPA’s Environmental Monitoring and Assessment  
6 Program Estuaries program (EMAP) and total developed land cover is from the 1992 National  
7 Land Cover Dataset (NLCD). We use a total of 112 stations. Hollister et al. (2008a) identified  
8 spatial extents with the strongest linear association with different sediment metals. Following  
9 suggestions in Hollister et al. (2008a), we define contributing watersheds as all land area within  
10 15 km or less from a station that also drains to that estuarine system. For this example, we define  
11 impaired ecological condition by any site that had at least one metal exceeding the Effects Range  
12 Median (ERM) value, a benchmark for potential effects on benthic biota (Long et al., 1995). A  
13 site with at least one metal exceeding the ERM value has been previously used as a measure of  
14 impairment (Paul et al., 1999). We use the metals examined in Hollister et al. (2008a). We  
15 expect to see higher amounts of developed lands within 15 km of stations that also have high  
16 concentrations of sediment metals. The probability of impairment should increase as the total  
17 amount of developed lands in the contributing watershed increases. Conversely, the probability  
18 of being impaired would become less as total amount of developed lands decreases.

19

## 20 **RESULTS AND DISCUSSION**

21

### 22 *Water Quality Criterion Example*

23           To ensure that CProb works as expected, we compare the CProb results to those obtained  
24 by Paul and McDonald (2005). With the Mid-Atlantic Highlands Data, the resultant CProb  
25 scatterplots (Figure 1a) and cumulative distribution function plots (Figure 1b) match Figures 3



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1 and 4 of Paul and McDonald (2005). The conditional probability plot from CProb (Figure 1c)  
2 very closely matches Paul and McDonald's (2005) Figure 5. As expected, the only differences  
3 are a product of the confidence intervals resulting from the different bootstrapped samples.

4

#### 5 *Landscape Example*

6       Of the 112 stations in the landscape example, 100 have no metals exceeding an ERM  
7 value (Figure 2a). On average, these sites have 6169 ha of developed land with a standard  
8 deviation of 8041 ha. The average size of the contributing watersheds (i.e., drainage within 15 km  
9 of the station) is 62,749 ha with a standard deviation of 7513 ha. CPA results for the landscape  
10 example corroborate past studies and suggest that higher amounts of developed land in  
11 contributing watersheds lead to poor condition in estuaries. Although separating developed land  
12 into finer classifications (e.g., industrial and residential) might yield stronger relationships, the  
13 accuracy of those finer classes is less than the documented accuracy of the coarser developed land  
14 classification and would lead to greater uncertainty (Yang et al., 2001; United States Geological  
15 Survey, 2003; Hollister et al., 2004). The cumulative distribution function indicates that the  
16 amount of developed land can discriminate between unimpaired sites (no metals greater than an  
17 ERM) and impaired sites (at least one metal greater than an ERM) as indicated by the separation  
18 between the two curves (Figure 2b). In fact 100% of all observed impaired sites have at least  
19 14000 ha of developed land in the contributing watershed (i.e., drainage within 15km of the  
20 sampling station). The unimpaired sites have a range of developed land between 51 and 43,000  
21 ha, but no sites with less than 14,000 ha of developed land have any metals exceeding an ERM  
22 value. Only 15% of the unimpaired sites have total developed land amounts that overlapped those  
23 of the bad sites (Figure 2b).

24       The conditional probability of impairment increases as total developed area in a  
25 watershed increases (Figure 2c). Non-overlapping confidence intervals (i.e., where the

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1 conditional confidence interval does not overlap the unconditional confidence interval) may be  
2 used as a conservative test for differences. The unconditional probability and confidence interval  
3 is represented by the first point in the conditional probability plot. In this case, non-overlapping  
4 confidence intervals suggest that the conditional probability of impairment is significantly higher  
5 between approximately 7500 ha and 37,500 ha than the unconditional probability of impairment  
6 of approximately 10% (i.e.,  $P(Y)$ ). This suggests that if development was limited to  
7 approximately 7500 ha or less within 15 km of a sampling station, the probability of metal  
8 contamination should not be significantly greater than what would be normally expected for this  
9 area. There are few stations with total developed land higher than 37,500 ha. The uncertainty  
10 about this part of the curve is large and thus it is not possible to draw any conclusions.

11

## 12 **CONCLUSIONS**

13 Our goals for this short communication were to describe a new tool for conducting  
14 Conditional Probability Analysis and illustrate its use with two examples: one to validate the  
15 results and one to show the versatility of the tool with an independent dataset. Our results  
16 validate the calculations and analyses from CProb as we reproduced the results of (Paul and  
17 McDonald, 2005). Furthermore, the power of CPA is that it provides a measure of the  
18 association between any two variables, environmental or otherwise, that explicitly incorporates  
19 uncertainty. Lastly, CProb is proving to be user friendly and is gaining acceptance with a number  
20 of state environmental managers in the Northeast. This tool along with the analytical techniques  
21 described here and in Paul and McDonald, (2005) are helping set scientifically defensible water  
22 quality criteria and more clearly describing stressor-response relationships.

23

## 24 **ACKNOWLEDGEMENTS**

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1 Table 1. Software sources and links.

<b>Software</b>	<b>Source</b>	<b>Link</b>
Excel 2003	Microsoft	<a href="http://office.microsoft.com/excel">http://office.microsoft.com/excel</a>
R	R Project for Statistical Computing	<a href="http://www.r-project.org">http://www.r-project.org</a>
R(D)Com Server and RExcel	Sunsite	<a href="http://rcom.univie.ac.at">http://rcom.univie.ac.at</a>

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1 Figure 1a. Scatterplot showing relationship between EPT Taxa and Bedded Sediments.

2

3 Figure 1b. Cumulative Distribution Function showing percentage of stations with a given amount,  
4 or more, of percent fines.

5

6 Figure 1c. Conditional probability plot showing probability of impairment in streams with a given  
7 percentage of fine material in the sediment. Solid lines indicate the 95% confidence intervals.

8

9 Figure 2a. Scatterplot showing relationship between number of metals exceed the Effects Range  
10 Median (ERM) and total developed land (ha) withing 15 km of EMAP stations.

11

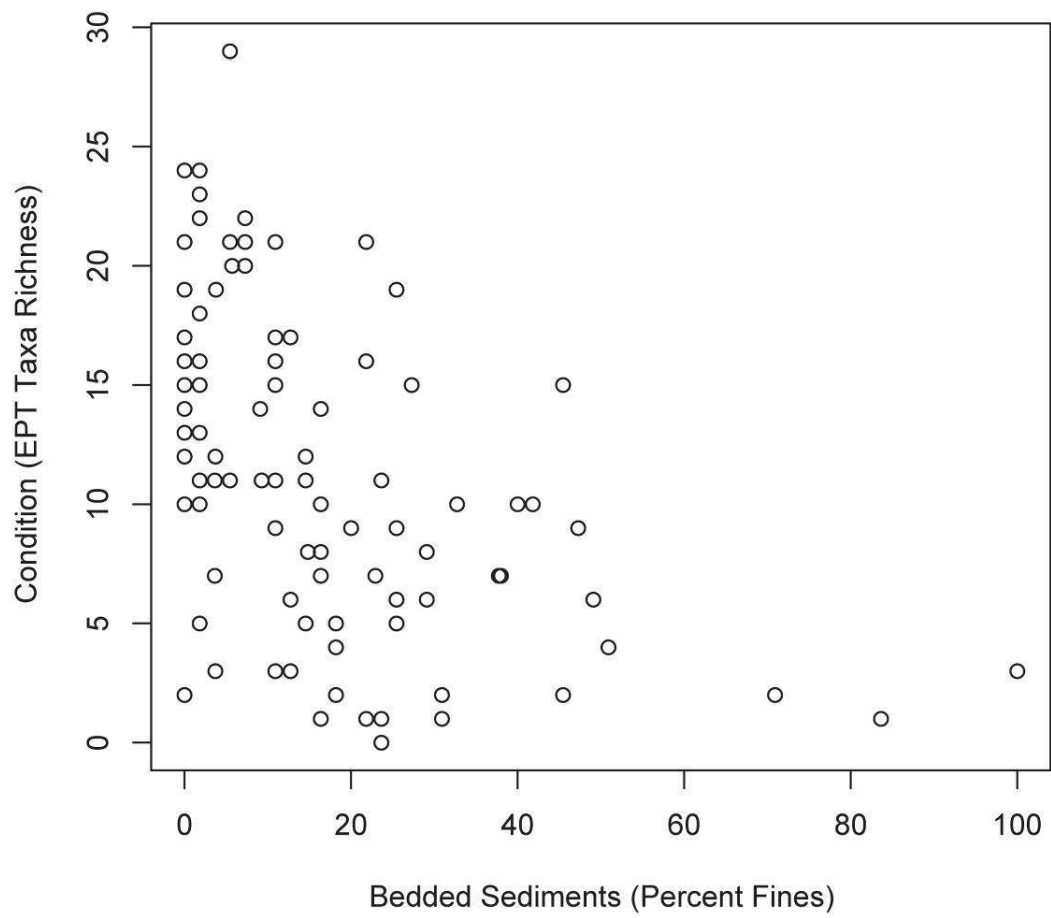
12 Figure 2b. Cumulative distribution function showing percentage of stations with a given amount,  
13 or more, of total developed land (ha) within 15 km of EMAP stations.

14

15 Figure 2c. Conditional probability plot showing probability of at least one metal exceeding the  
16 ERM given the total developed land (ha) is greater than or equal to  $X_c$ .

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Figure 1A; Q07-0536; J.W. Hollister



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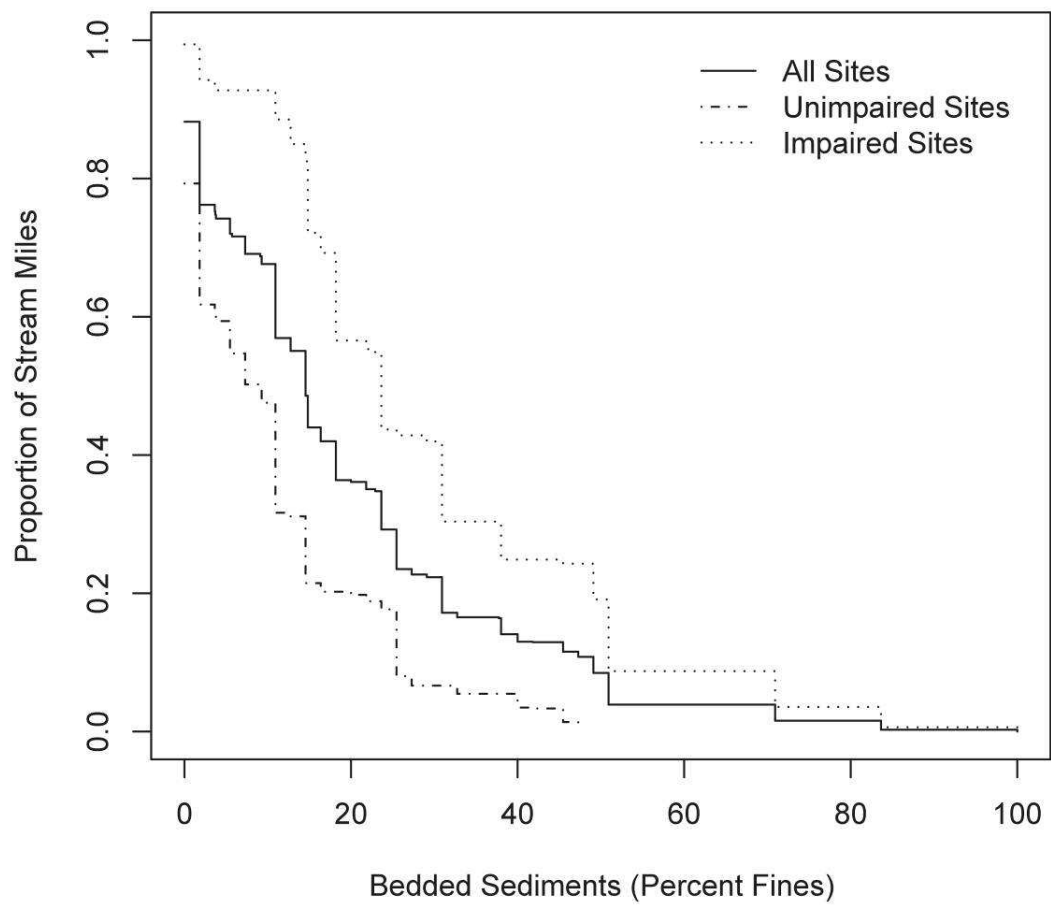
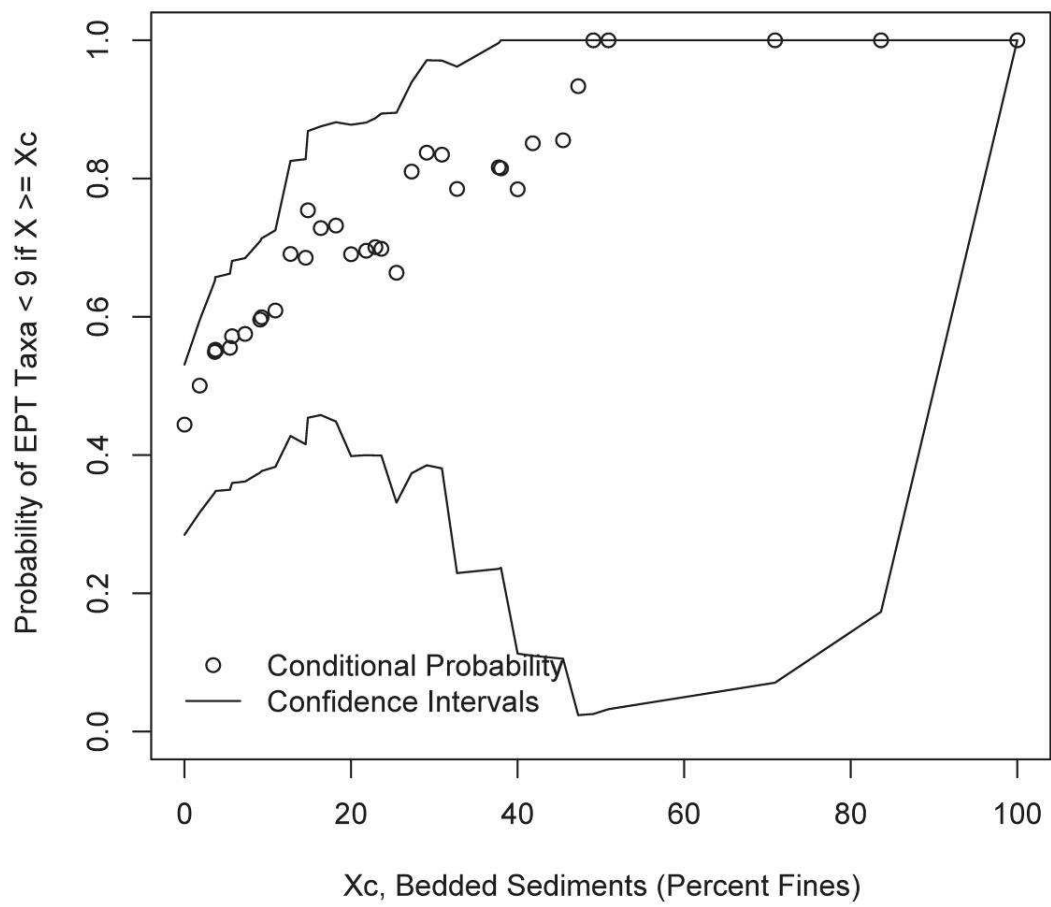
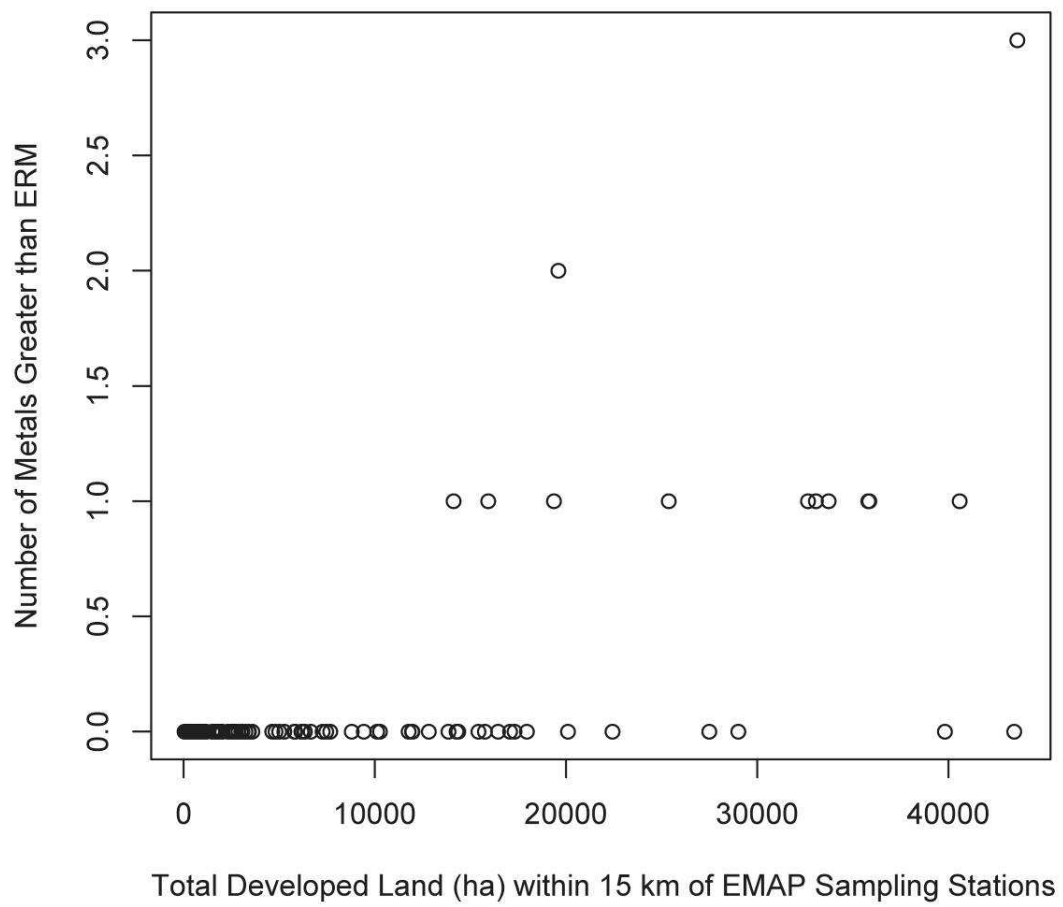


Figure 1C; Q07-0536; J.W. Hollister



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Figure 2A; Q07-0536; J.W. Hollister



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Figure 2B; Q07-0536; J.W. Hollister

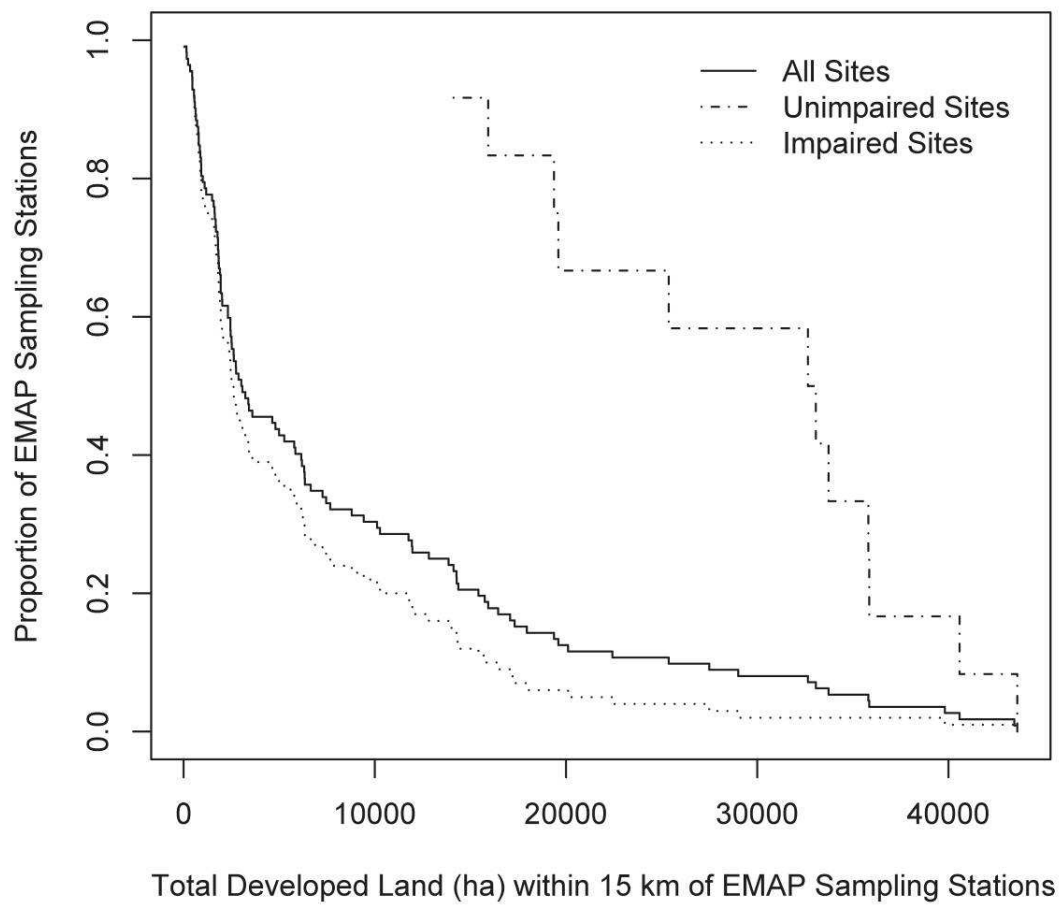


Figure 2C; Q07-0536; J.W. Hollister

